$$\frac{1}{n} + \log n \leq \sum_{k=1}^{n} \frac{1}{k} \leq 1 + \log n\,, \qquad (\forall n \in \mathbb{N})\,,$$