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**An amalgamated duplication of a ring along an ideal: the basic properties. (English summary)**

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In this article the authors introduce a new ring construction, built out of a ring  $R$  and an  $R$ -module  $E$ , called the amalgamated duplication of  $R$  along  $E$ . Section 2 discusses the main properties of the amalgamated duplication in relation to pullback-type constructions. Section 3 considers the case where  $E$  is an ideal of  $R$ , and pays special attention to ideal theoretic properties and topological structure of prime ideals of the amalgamated duplication in this particular case.

Reviewed by *Sarah Glaz*

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